On a stormy night, ten guests came to a dinner party. They left their shoes in the hall to keep the carpet clean. After dinner there was a blackout, and the guests, leaving one by one, put on at random any matching pair of shoes that was big enough to fit their feet.

Any guest who couldn't find a pair of shoes big enough spent the night.

What is the largest number of guests who might have had to spend the night?