## Summary on Lecture 4, April 1st 2016

## Finite State Machines: More examples.

(7) Delay machine. Now we describe a finite state machine which delays the sequence by putting first k zeros. For example, if k = 1, the input sequence 11110111101110110... gives the following output

## $\begin{array}{c} 11110111110111010110...\\ 011110111110111010110...\end{array}$

Here is the diagram describing the functions  $\nu$  and  $\omega$ :



The case k = 2 is essentially more complicated since the machine has to remember two previous digits. Here the input sequence 11110111101110110... gives the output 001111011101101010... Here is the diagram describing the functions  $\nu$  and  $\omega$ :



We notice that the states  $s_0, s_1, s_2$  have only 0 as an output, and the states  $s_3, s_4, s_5, s_6$  "remember" the prior inputs 00, 10, 10, 11 respectively.

**Exercise.** Construct a delay machine with k = 3.